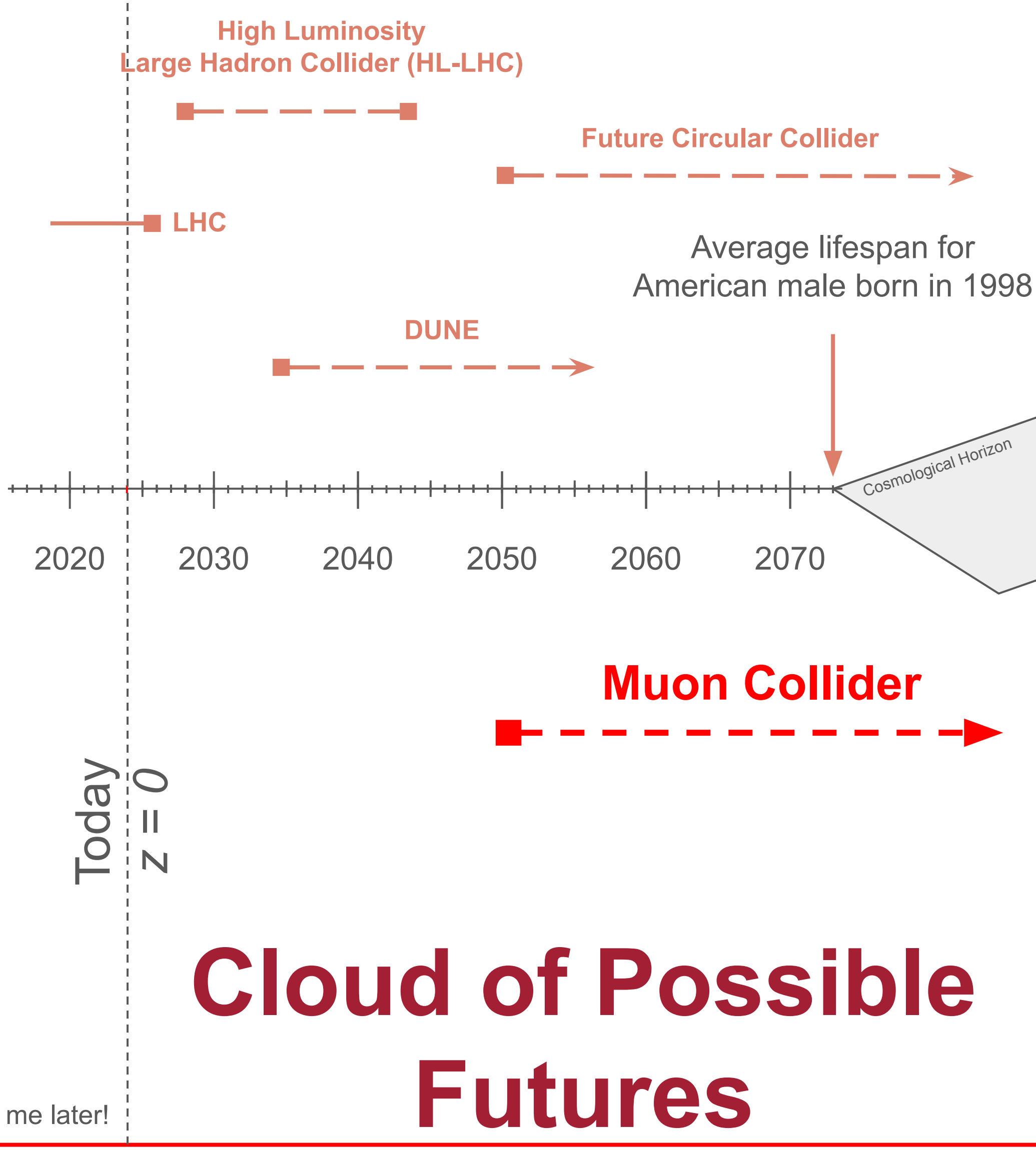
The New Physics Case for Muon Beam-Dump Experiments

Rikab Gambhir

Email me questions at rikab@mit.edu!
Based on [Cesarotti, **RG**, 2310.16110]

A **muon collider** is an exciting future prospect for our community!

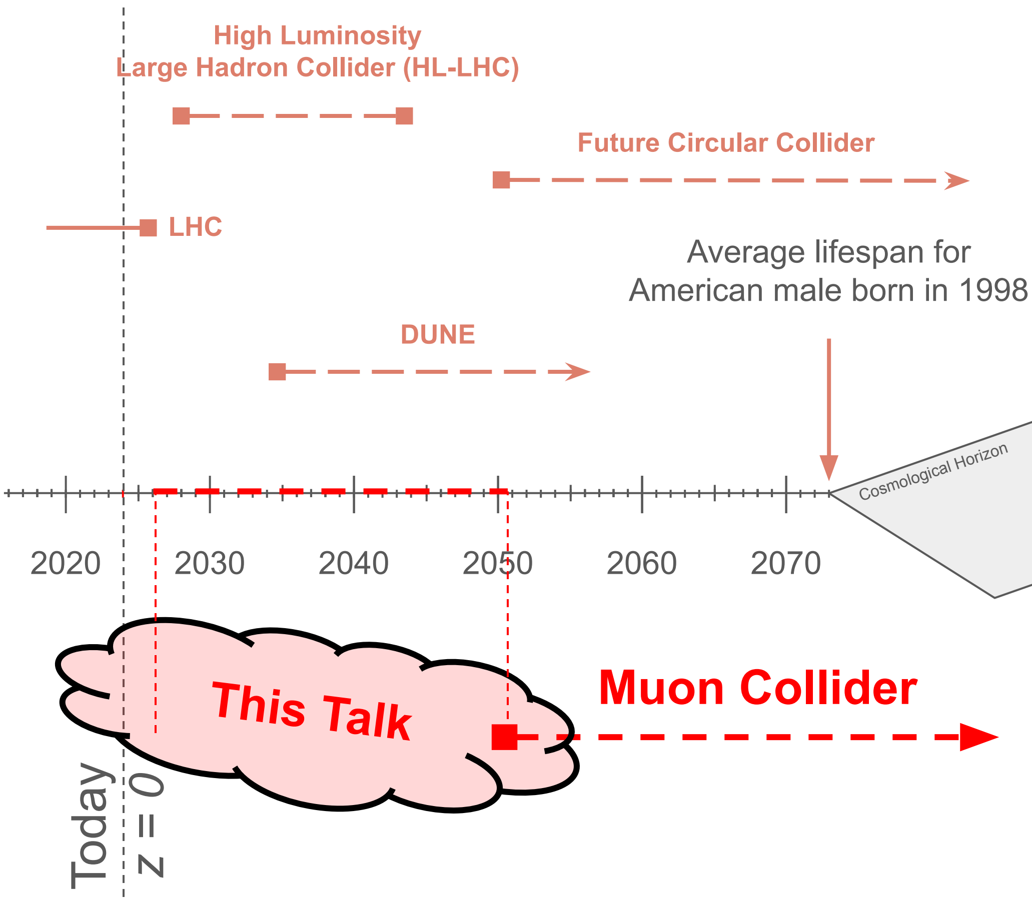


Cloud of Possible Futures

Why are muons so great? Ask me later!

A **muon collider** is an exciting future prospect for our community!

… but muons are hard to collide. What can we do ***now***?



Cloud of Possible Futures

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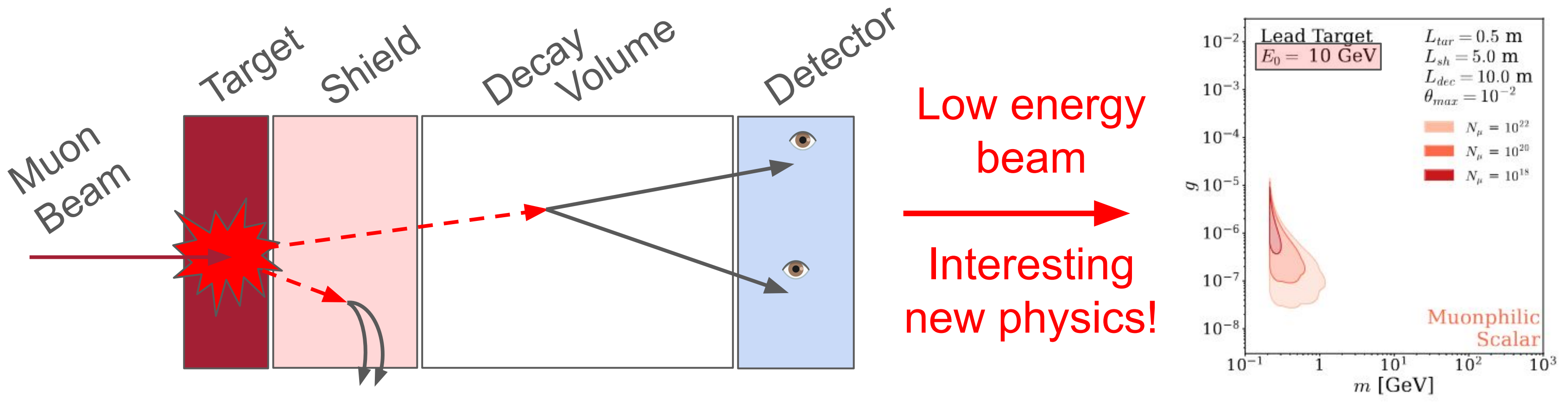
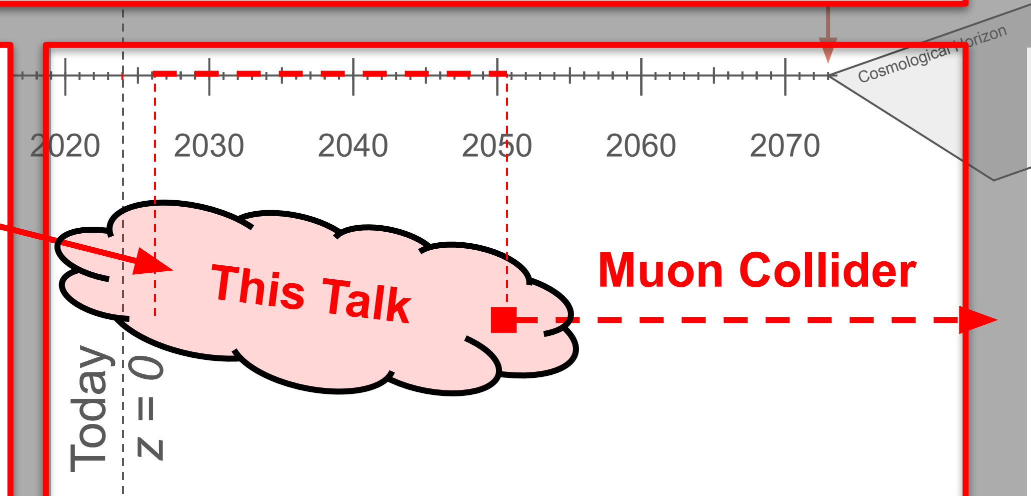


Road to the Future

Lots of R&D needed! A huge undertaking …

This Talk: R&D is worth it, because **muon test beams** already have the potential for discovering **new physics**! Interesting results for muon beams as low as **10 GeV**!

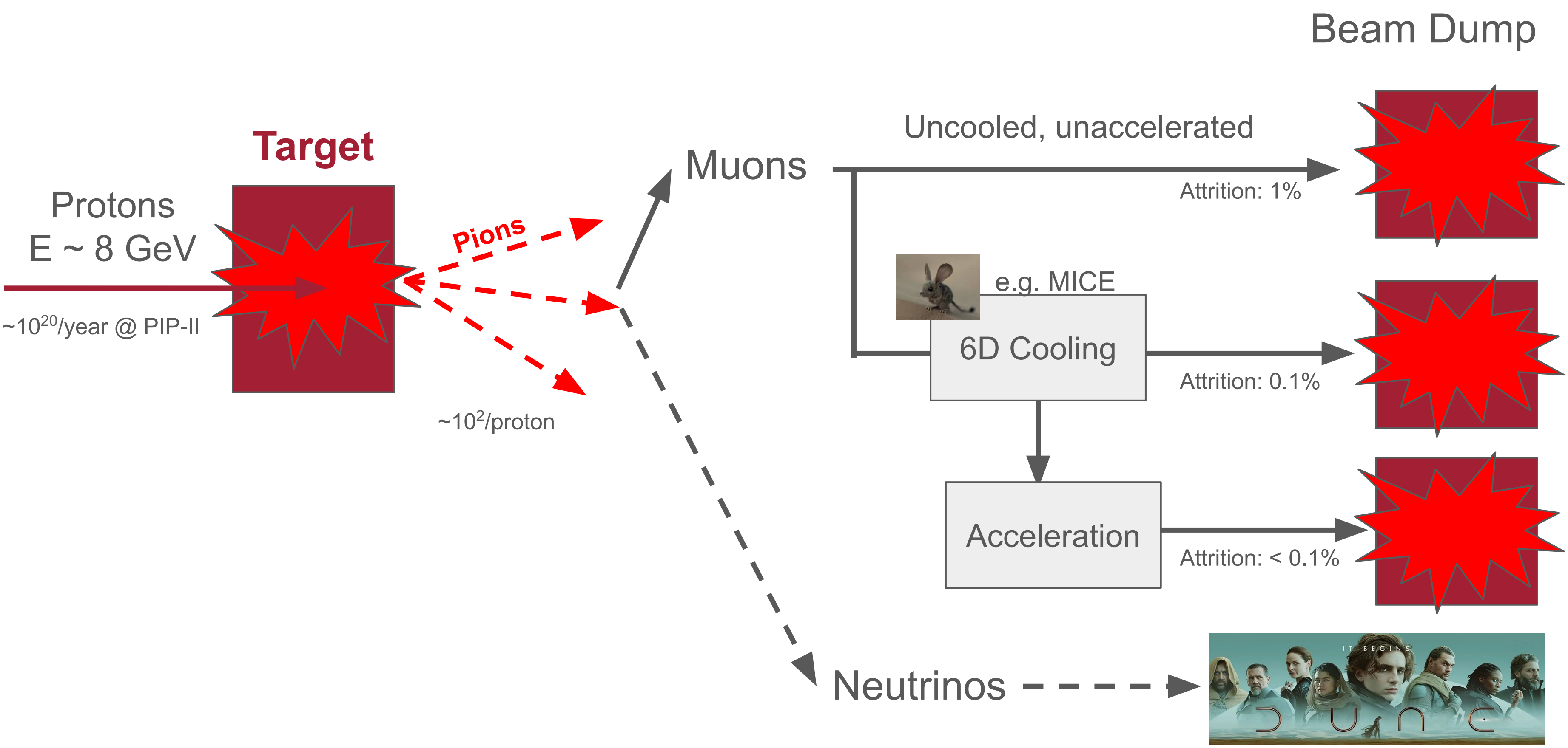


Cloud of Possible Futures

Why are muons so great? Ask me later!

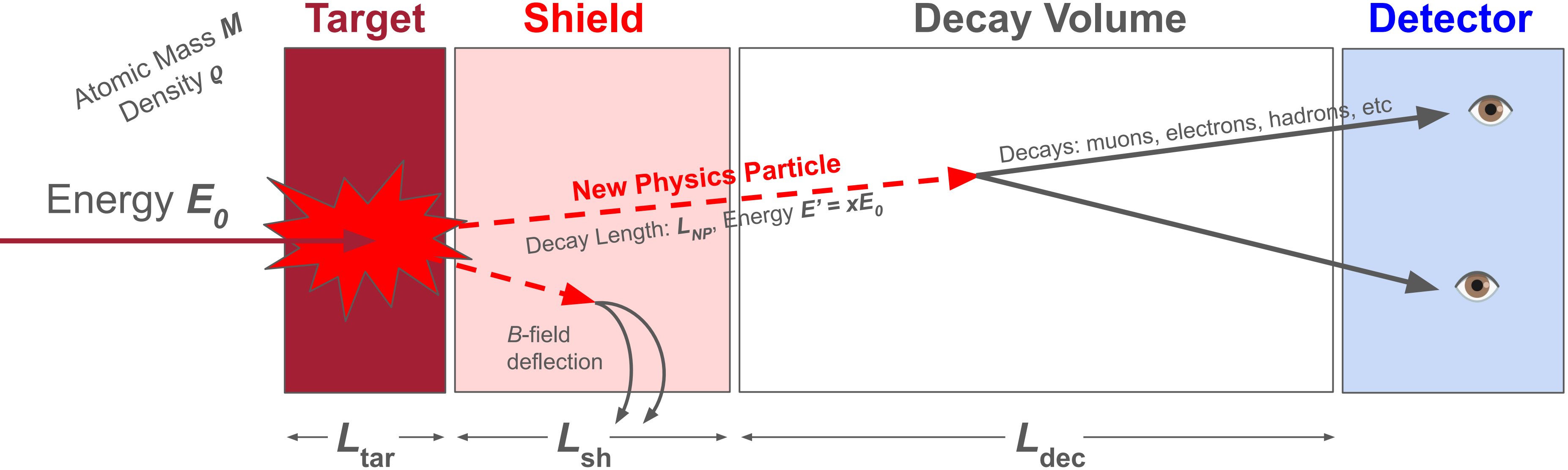
Source: **How are Muons Born?**

Using PIP-II at Fermilab as a template…



Number of **muons on target**, 10^{18} - 10^{22} / year

Beam Dump Fundamentals



Produce weakly coupled, long lived new particles with a large boost!
Junk (residual muons, SM decays, etc) deflected and/or absorbed by shield

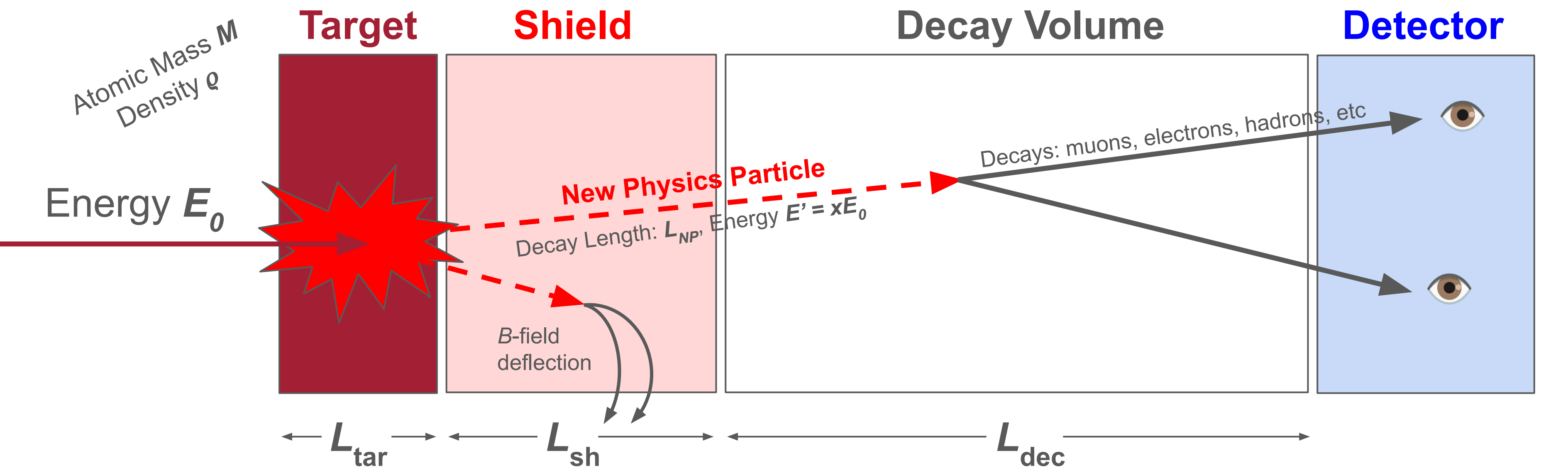
Nominal COM Energy: $\sqrt{s} = \sqrt{2E_0 M}$

Particles can travel a long distance: $l_{\mathrm{NP}} \approx \left(\frac{E_0}{\mathrm{TeV}}\right) \times \left(\frac{g}{10^{-6}}\right)^{-2} \times \left(\frac{m_{\mathrm{NP}}}{10\ \mathrm{MeV}}\right)^{-2} \times 100\mathrm{m}$

Beam Dump Fundamentals

How many new physics particles do we expect to see? Depends on target, cross section, experiment geometry, and total number of muons:

$$\frac{dN}{dx} = N_\mu \frac{N_0 \rho l_0}{A} \frac{d\sigma}{dx} \left(e^{\frac{L_{\rm tar}}{l_{\rm NP}}} - 1 \right) e^{-(L_{\rm tar} + L_{\rm sh})} \left(1 - e^{-L_{\rm dec}/l_{\rm NP}} \right)$$

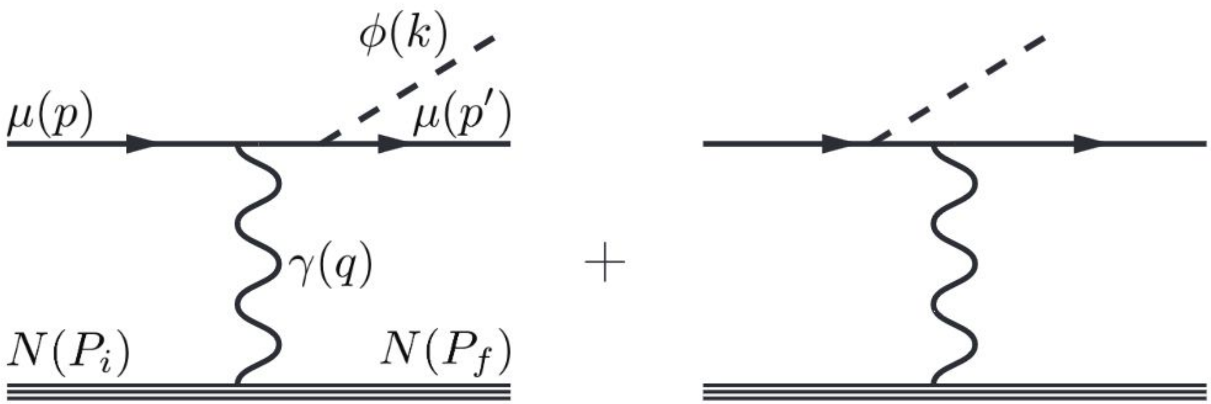


New Physics – Bremsstrahlung Production

Given a beam dump, what kind of new physics ϕ can we search for?

$$\mu(p) + N(P_i) \to \mu(p') + N(P_f) + \phi(k)$$

Where ϕ is either spin-0 or spin-1 and either parity-even or parity-odd

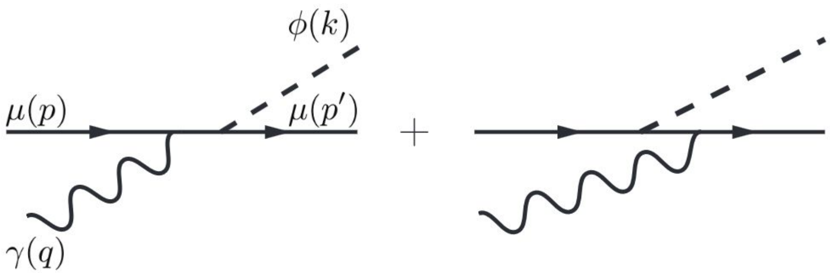


*Fully collinear approximation begins to fails for E < 100 GeV – see 2310.16110 for the full treatment and long formulas.

Cross Sections – Calculation

Simplify the calculation … use Weizsäcker-Williams!

$$\mu(p) + \gamma(q) \to \mu(p') + \phi(k)$$



Approximation works best when the photon (virtuality t) is nearly on shell:

$$t_{\mathrm{min}} \approx \left(\frac{m_\phi^2}{2E}\right)^2$$

Sets the minimum beam energy we consider

Enhanced production when t is small – collinear emission, regulated by masses

$$\left(\frac{d\sigma_{2\to 3}}{dx}\right)_{\mathrm{IWW}} = \frac{g^2}{2\pi}\alpha\chi\frac{|\vec{k}|}{E}\frac{(1-x)}{x}\int_{-\infty}^{\tilde{u}_{\mathrm{max}}} d\tilde{u}\frac{\mathcal{A}^{22}_{t=t_{\mathrm{min}}}}{\tilde{u}^2}$$

Spin-averaged squared amplitude evaluated at t_{min}

Integrated Photon Flux

$$\chi \equiv \int_{t_{\mathrm{min}}}^{t_{\mathrm{max}}} dt\frac{t - t_{\mathrm{min}}}{t^2}G(t)$$

$$\tilde{u}(x,\theta) \approx -xE_0^2\theta^2 - m_X^2\frac{1-x}{x} - m_\mu^2 x$$

Models

Today, I will only talk about these two.
Ask me after about other models!

Scalar

$$\mathcal{L}^S_{\text{int}} \supset -i g_S \phi \bar{\psi} \psi$$

e.g. muonphilic, leptophilic scalars

Pseudoscalar

$$\mathcal{L}^P_{\text{int}} \supset -i g_P a \bar{\psi} \gamma^5 \psi$$

e.g. muonphilic, leptophilic pseudoscalars*

Vector

$$\mathcal{L}^V_{\text{int}} \supset -i g_V V_\mu \bar{\psi} \gamma^\mu \psi$$

e.g. Dark Photons, L_μ - L_τ

Axial Vector

$$\mathcal{L}^A_{\text{int}} \supset -i g_A A_\mu \bar{\psi} \gamma^\mu \gamma^5 \psi$$

e.g. muonphilic axial vectors

*ALPs are funny in our setup.

Models

Scalar

$$\mathcal{L}^S_{\text{int}} \supset -ig_S \phi \bar{\psi} \psi$$

e.g. muonphilic, leptophilic scalars

Vector

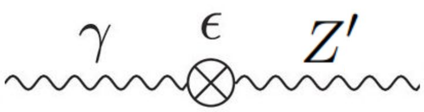
$$\mathcal{L}^V_{\text{int}} \supset -ig_V V_\mu \bar{\psi} \gamma^\mu \psi$$

e.g. Dark Photons, L_μ - L_τ

Dark Photons

Extend the SM with a broken *U*(1)' symmetry with a gauge boson *Z*'.

Couples to SM charged particles via kinetic mixing with the photon with parameter ε.



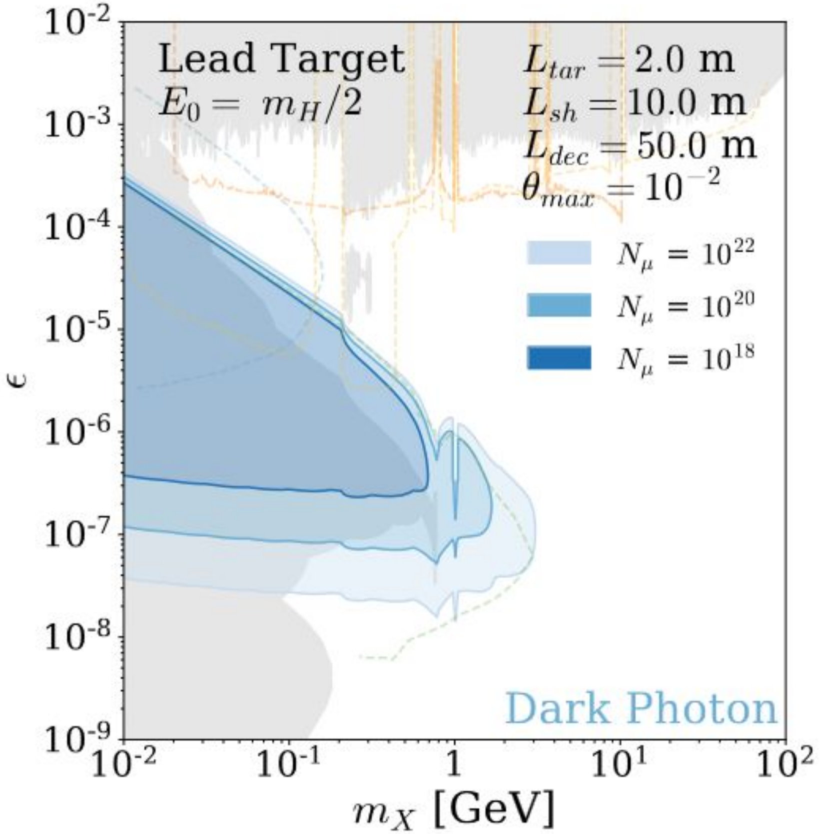
$$\mathcal{L} \supset \frac{1}{2} m^2_{Z'} Z'^\mu Z'_\mu - \sum_{l \in e,\mu,\tau} i\epsilon e \left(\bar{l}\gamma^\mu l\right) Z'_\mu$$

Classic DM candidate!

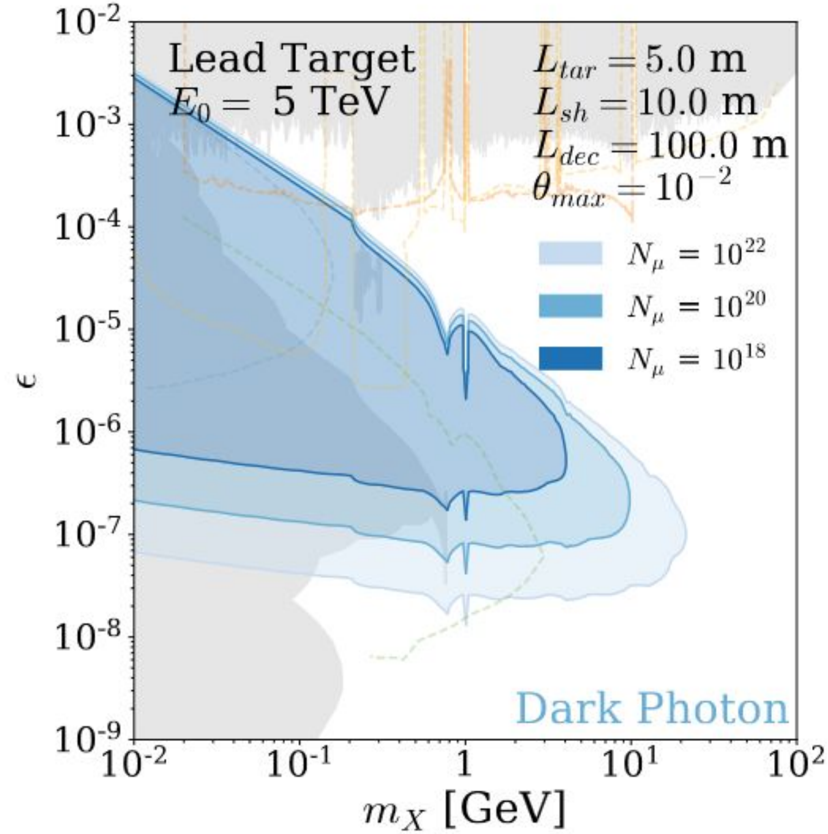
Dark photons are like light, except they're dark instead of light, and heavy instead of light

*ALPs are funny in our setup.

Results – Dark Photons



(a) Dark photon limits at $E_0 = m_h/2$.



(b) Dark photon limits at $E_0 = 5$ TeV.

Models

Scalar

$$\mathcal{L}^S_{\text{int}} \supset -ig_S \phi \bar{\psi} \psi$$

e.g. muonphilic, leptophilic scalars

Vector

$$\mathcal{L}^V_{\text{int}} \supset -ig_V V_\mu \bar{\psi} \gamma^\mu \psi$$

e.g. Dark Photons, L_μ - L_τ

Muonphilic

Model where the new scalar *only* couples to muons.

$$\mathcal{L} \supset \frac{1}{2} m_\phi^2 \phi^2 - i\left[g_\mu \bar{\mu}\mu + \cancel{g_e \bar{e} e} + \cancel{g_\tau \bar{\tau}\tau}\right] \phi$$

Can be generated by the dim 5 operator:

$$\phi L H \mu^c$$

Can also arise as a Higgs-like coupling with $g_\ell \sim m_\ell / \Lambda$ with:

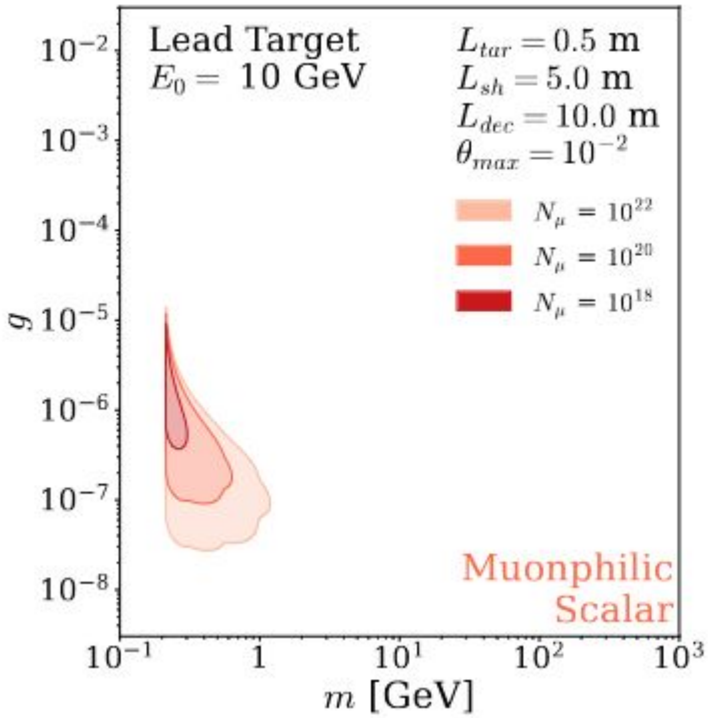
$$m_e \ll m_\mu \text{ and } m_\phi < m_\tau$$

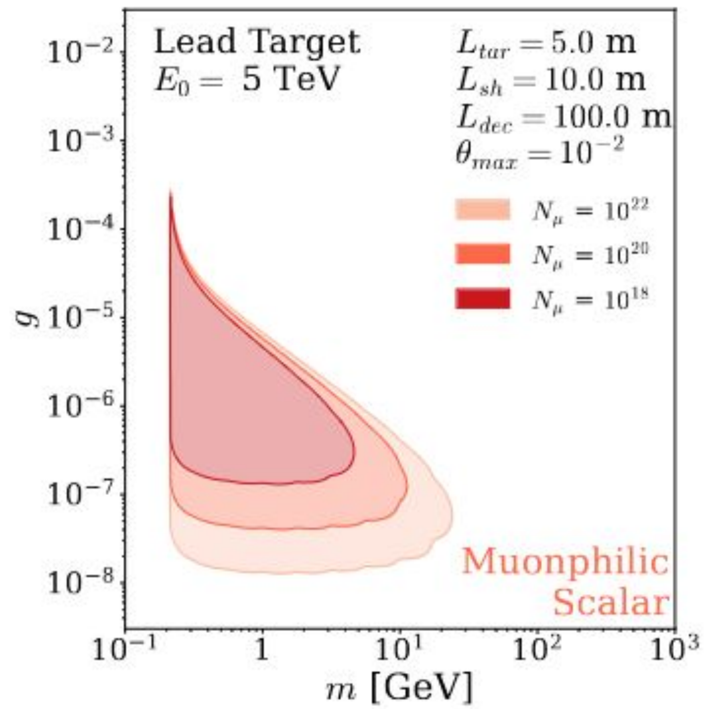
Muonic experiments probe muonic couplings!

See [1902.07715] for example UV completions
Can arise in e.g. Type III 2HDM

*ALPs are funny in our setup.

Results – Muonphilic

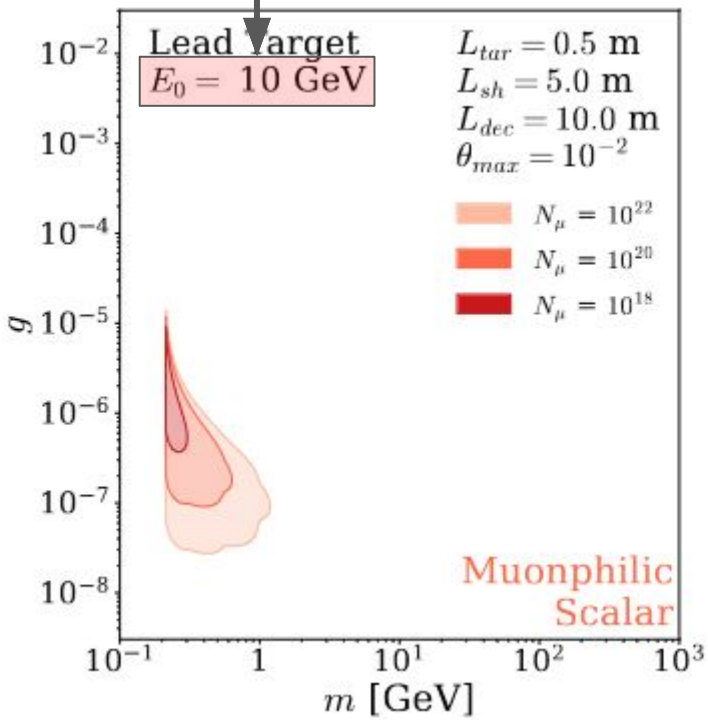


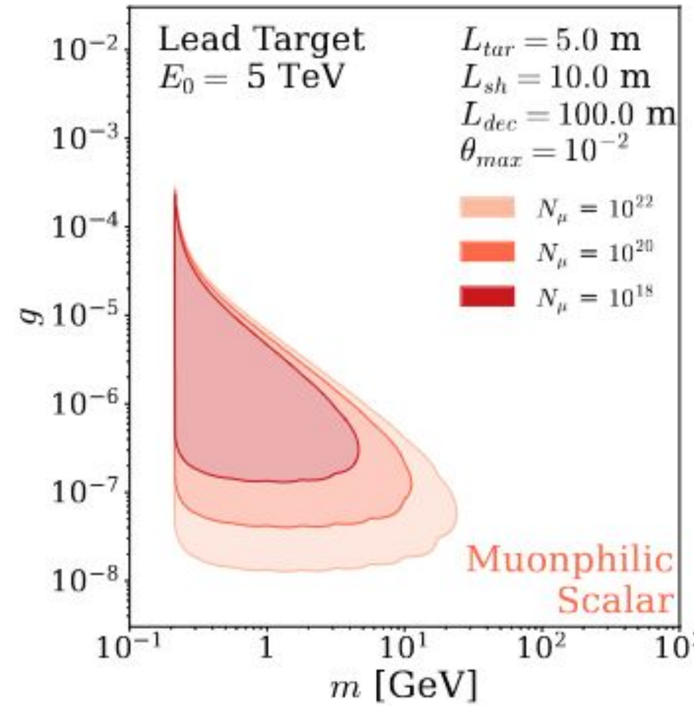


Muon specific coupling, **no other limits** in this range!

Results – Muonphilic

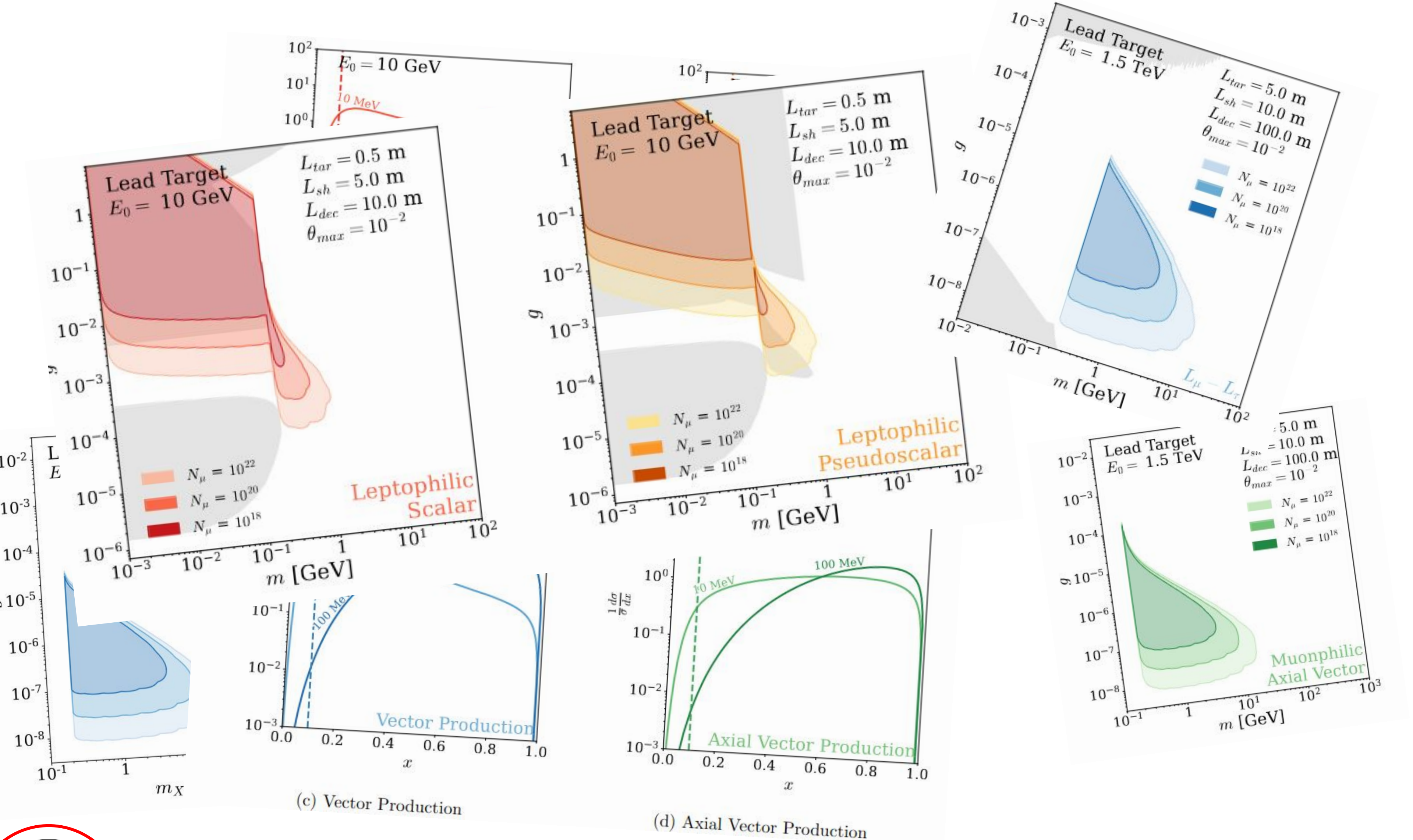
10 GeV … possible at a near-term **demonstrator facility**!





Muon specific coupling, **no other limits** in this range!

Results – Lots of models!



Results – Lots of models!

Lots of Possibilities!

Considerations

To obtain these results, we have made a lot of *conservative* simplifying assumptions – can do much better with a thorough experimental analysis!

- **Detector**: We assume a binary “Did you see a particle or not?”. Much better sensitivity / background rejection achievable with tracking, calorimetry, timing … !
- **Thin Targets**: We assumed the target is thin to simplify material calculations. This can be relaxed to increase the interaction volume!
- **Other visible signatures**: We only considered electrons, muons, and hadrons as visible final states. But other signatures (photons, MET, secondary decays) are possible!

A thorough analysis and simulation is required!

Considerations

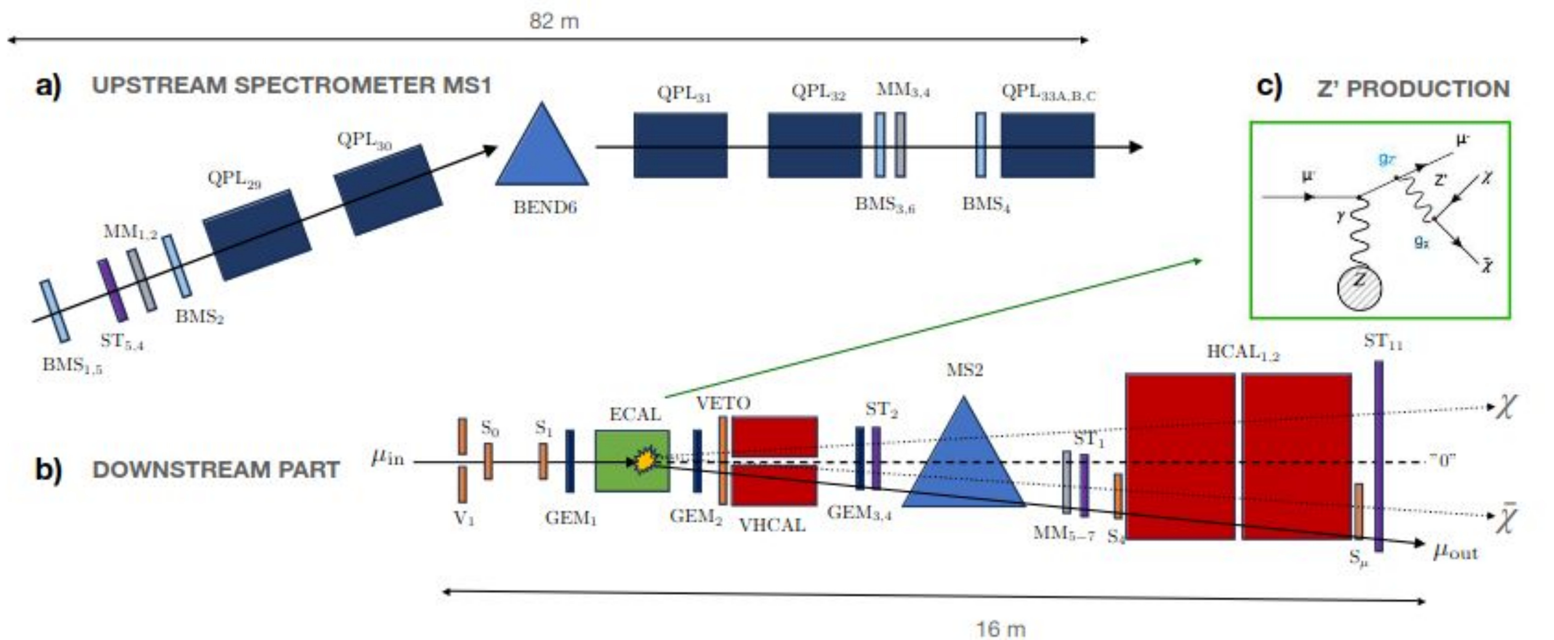
Muon Beams are real!

~160 GeV, 10^{10} Muons

[NA64μ, 2401.01708]

Earlier this year (Jan 2024)

Exploration of the Muon $g-2$ and Light Dark Matter explanations in NA64 with the CERN SPS high energy muon beam

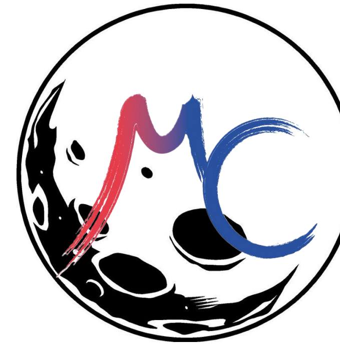


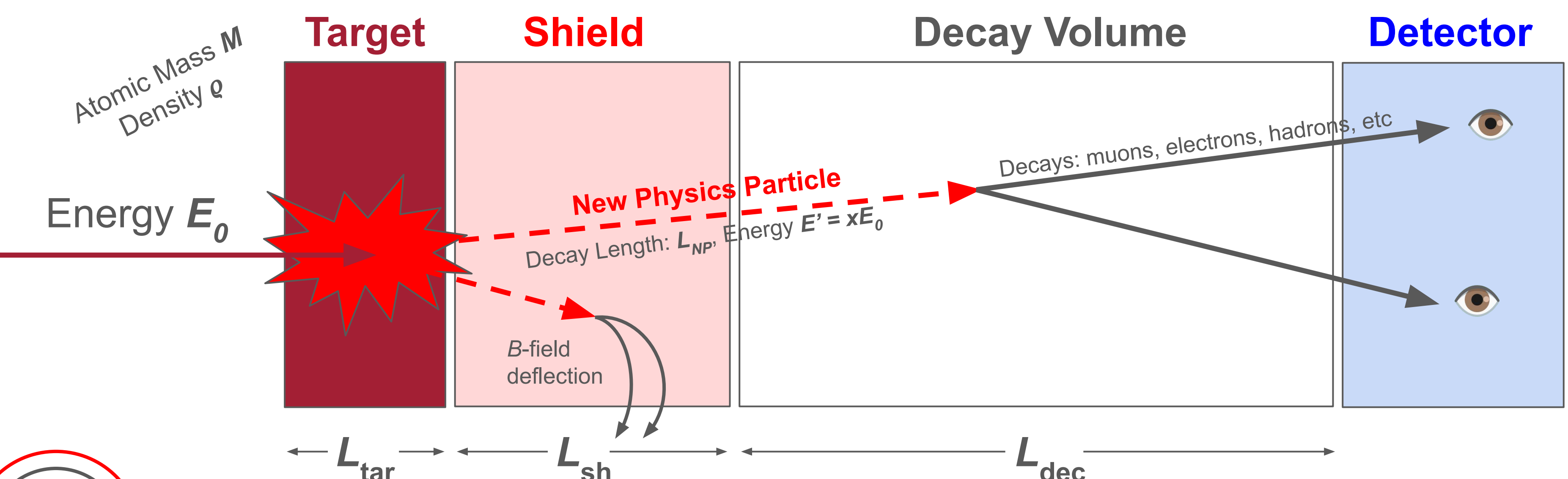
Conclusion

A **muon beam-dump experiment** provides an excellent opportunity for **new physics** on the road to a **muon collider**

New physics is possible ***in the next few years*** with as low as a **10 GeV** muon beam at a demonstrator facility! We don't need to wait.

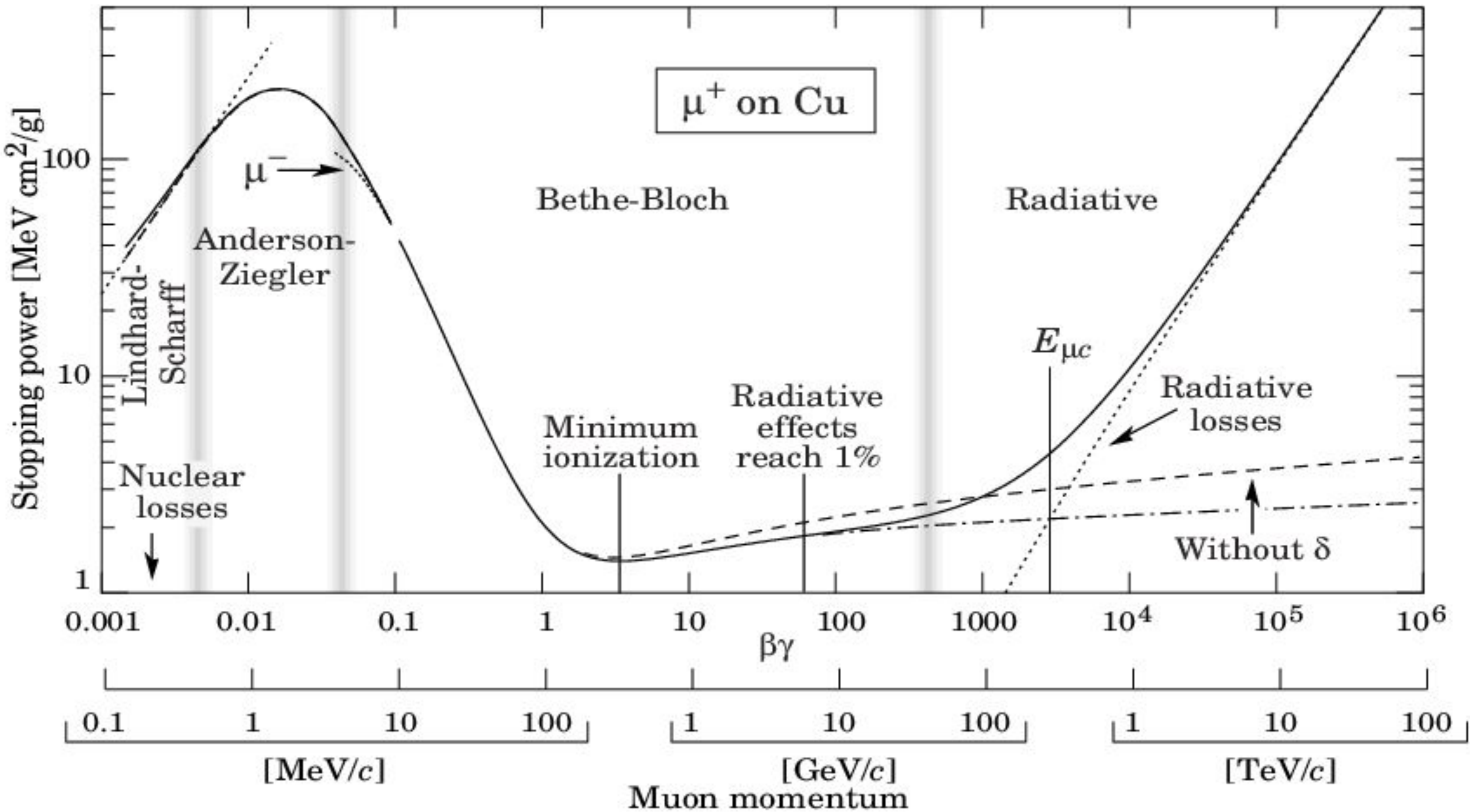
"This is our Muon Shot"





Appendices

Muon Stopping Power



Full Cross Section Formulas

$$\left(\frac{d\sigma_{2\to3}(p+P_i\to p'+k+P_f)}{d(p\cdot k)d(k\cdot P_i)}\right)_{\rm WW}=\left(\frac{\alpha\chi}{\pi}\right)\left(\frac{E_0 x\beta_\phi}{1-x}\right)\times\left(\frac{d\sigma_{2\to2}(p+q\to p'+k)}{d(p\cdot k)}\right)_{t=t_{\rm min}}$$

$$\left(\frac{d\sigma_{2\to3}}{dx\,d\cos\theta}\right)_{\rm WW}=\frac{g^2}{2\pi}\alpha|\vec{k}|E(1-x)\frac{\mathcal{A}^{22}_{t=t_{\rm min}}}{\tilde{u}^2}\chi$$

$$\mathcal{A}^{2\to2}_{S,t=t_{\rm min}}\approx\frac{x^2}{1-x}+2(m_\phi^2-4m_\mu^2)\frac{\tilde{u}x+m_\mu^2(1-x)+m_\mu^2x^2}{\tilde{u}^2}$$

$$\mathcal{A}^{2\to2}_{P,t=t_{\rm min}}\approx\frac{x^2}{1-x}+2m_a^2\frac{\tilde{u}x+m_\mu^2(1-x)+m_\mu^2x^2}{\tilde{u}^2}$$

$$\mathcal{A}^{2\to2}_{V,t=t_{\rm min}}\approx2\frac{2-2x+x^2}{1-x}+4(m_V^2+2m_\mu^2)\frac{\tilde{u}x+m_\mu^2(1-x)+m_\mu^2x^2}{\tilde{u}^2}$$

$$\mathcal{A}^{2\to2}_{A,t=t_{\rm min}}\approx\frac{4m_\mu^2x^2}{(m_A^2)(1-x)}+2\frac{2-2x+x^2}{1-x}+4(m_A^2-4m_\mu^2)\frac{\tilde{u}x+m_\mu^2(1-x)+m_\mu^2x^2}{\tilde{u}^2}$$

Beam Dump Fundamentals (Details)

How many new particles should we expect to see*?

$$\frac{dN}{dxdz} = N_\mu \frac{N_0 X_0}{A} \times \mathcal{BR} \times \int_{E_\phi}^{E_0} \frac{dE'}{E'} \int_0^T dt\; I(E'; E_0, t) \times E_0 \frac{d\sigma}{dx'}\bigg|_{x' \equiv E'/E_0} \frac{dP(z - \frac{X_0}{\rho} t)}{dz}$$

*Assuming that the detector is wide enough to capture all emitted particles – we have chosen geometries and cutoffs such that this is approximately true.
*Assuming 100% detection efficiency.
*Assuming no SM backgrounds, taken care of by shields and/or absorption.

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Number of detected particles ***N*** as a function of their energy fraction ***x*** and decay length ***z***

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Beam Dump Fundamentals (Muon Source)

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Number of **muons on target**, 10^{18} - 10^{22} / year

Beam Dump Fundamentals (Target)

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N_0: Avogadro's Number, ~10^{23}/mol
X_0: Material Decay Length
A: Material atomic mass, ~10-100 g/mol

$I(E'; E_0, t)$ = Radiative losses as the muon transverses a distance *t* through the target

Beam Dump Fundamentals (Target)

How many new particles should we expect to see?

$$\frac{dN}{dx\,dz} = N_\mu \frac{N_0 X_0}{A} \times \mathcal{BR} \times \int_{E_\phi}^{E_0} \frac{dE'}{E'} \int_0^T dt\, I(E'; E_0, t) \times E_0 \frac{d\sigma}{dx'}\bigg|_{x' \equiv E'/E_0} \frac{dP(z - \frac{X_0}{\rho} t)}{dz}$$

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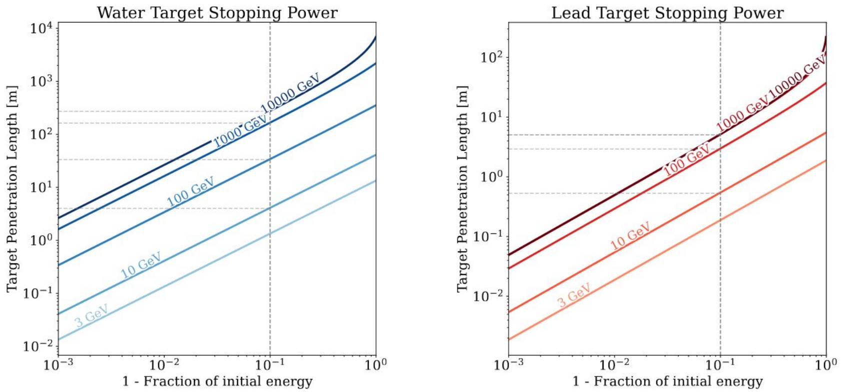

Radiative losses for water and lead

Thin Target Approximation: No losses

$$I(E'; E_0, t) = \delta(E' - E_0)$$

Fixes the size of L_{tar}, otherwise requires more sophisticated material modeling …

Beam Dump Fundamentals (Decays)

How many new particles should we expect to see?

$$\frac{dN}{dxdz} = N_\mu \frac{N_0 X_0}{A} \times \mathcal{BR} \times \int_{E_\phi}^{E_0} \frac{dE'}{E'} \int_0^T dt\, I(E'; E_0, t) \times E_0 \frac{d\sigma}{dx'}\bigg|_{x' \equiv E'/E_0} \frac{dP(z - \frac{X_0}{\rho} t)}{dz}$$

Branching ratio into ***visible* final states** (electrons, muons, hadrons)*

Probability of the new particle decaying at a (normalized) position *z*

$$\frac{dP(l)}{dl} = \frac{1}{L_{\rm NP}} e^{-l/L_{\rm NP}}$$

*Photons not considered, but definitely possible to do in other setups!
*Hadrons obtained by using *R*-ratio measurements, OK below *Z* pole.
* Tau decays are possible, but to be conservative we will assume we can't reconstruct them.

Beam Dump Fundamentals (Decays)

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Probability of the new particle decaying at a (normalized) position *z*

$$\frac{dP(l)}{dl} = \frac{1}{L_{\rm NP}} e^{-l/L_{\rm NP}}$$

$$\Gamma_{\phi\to l^+l^-} = g_S^2 \frac{m_\phi}{8\pi}\left(1-\frac{4m_l^2}{m_\phi^2}\right)^{3/2}$$

$$\Gamma_{a\to l^+l^-} = g_P^2 \frac{m_\phi}{8\pi}\left(1-\frac{4m_l^2}{m_\phi^2}\right)^{1/2}$$

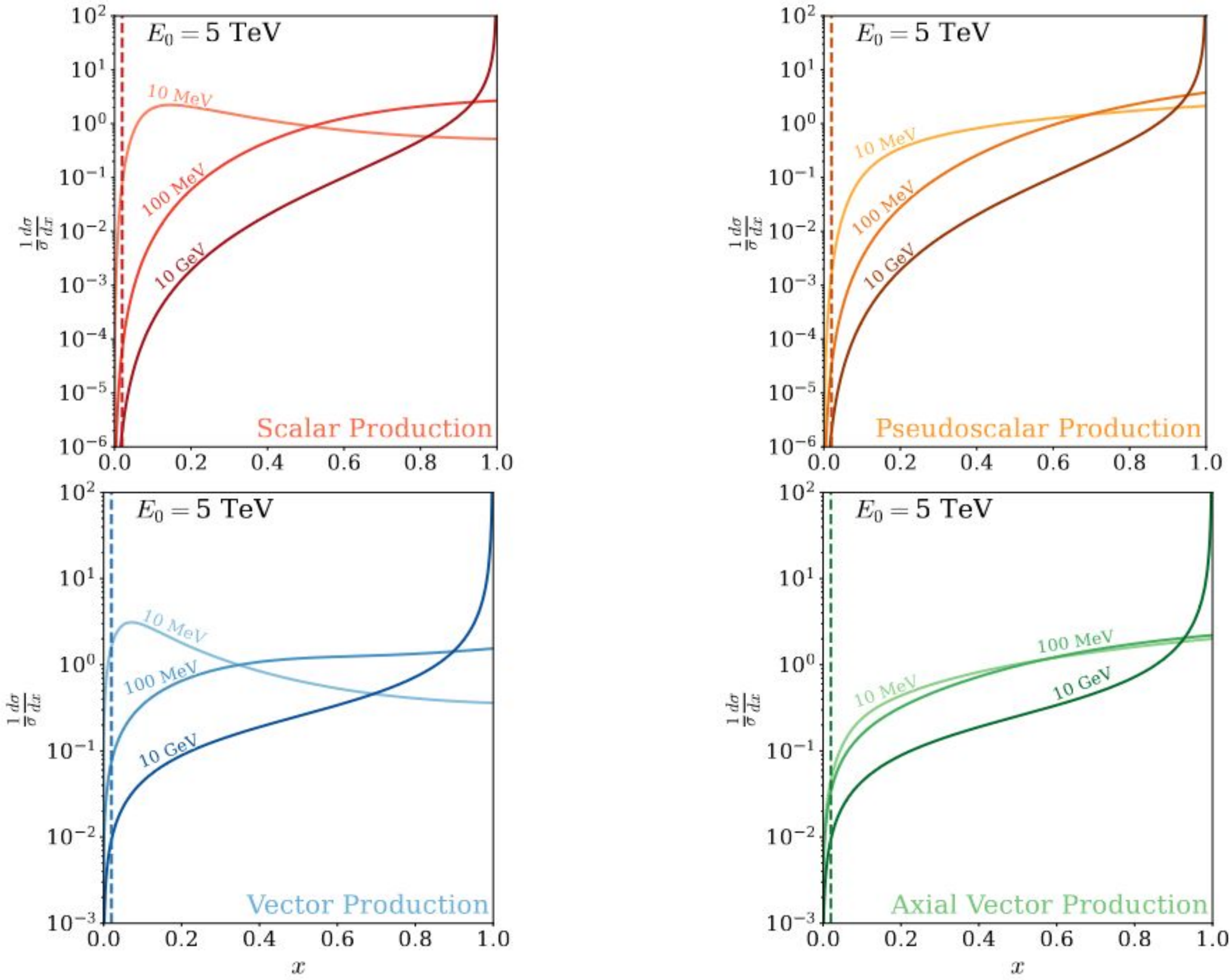
$$\Gamma_{V\to l^+l^-} = g_V^2 \frac{m_\phi}{12\pi}\left(1+\frac{2m_l^2}{m_\phi^2}\right)\left(1-\frac{4m_l^2}{m_\phi^2}\right)^{1/2}$$

$$\Gamma_{A\to l^+l^-} = g_A^2 \frac{m_\phi}{12\pi}\left(1-\frac{4m_l^2}{m_\phi^2}\right)^{3/2}.$$

Decay lengths and branching ratios depend on new particle mass, coupling, and spin/parity

*Photons not considered, but definitely possible to do in other setups!
*Hadrons obtained by using *R*-ratio measurements, OK below *Z* pole.
* Tau decays are possible, but to be conservative we will assume we can't reconstruct them.

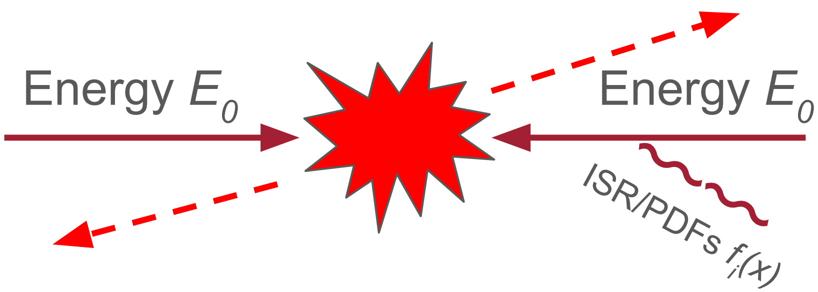
Models – Cross Sections



Beam Dump Fundamentals

Collider Setup

e.g. LHC, LEP, FCC

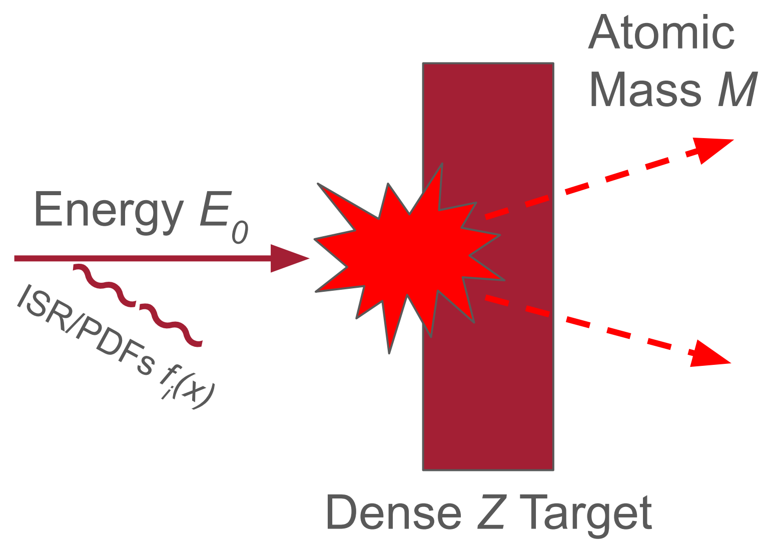


Nominal
Collision Energy: $\sqrt{s} = 2E_0$

- ✓ High Energies
- ✓ *s*-channel production

Beam Dump Setup

e.g. NA64, KEK, Orsay, E137, **Our Proposal**



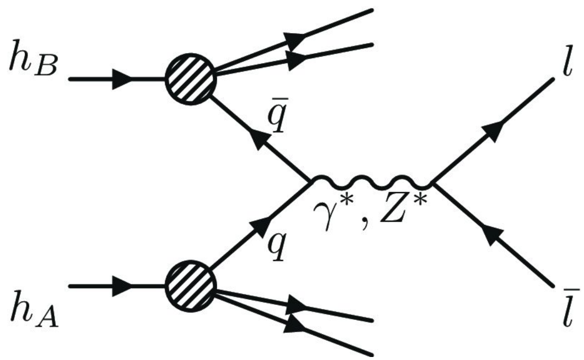
Nominal
Collision Energy: $\sqrt{s} = \sqrt{2E_0M}$

- ✓ Large rate
- ✓ Low couplings
- ✓ More cost effective

*This is just the *nominal* energy – PDFs can *drastically* change the actual hard process energy, especially for hadrons!

Aside: PDFs, ISR, and FSR

Since particles radiate or can be non-perturbative, it is a lot easier to think about colliding **partons** instead.



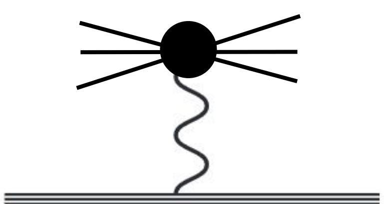
$$\sigma = \sum_{a,b} \int_0^1 \mathrm{d}x_a \mathrm{d}x_b \int f_{a/h_1}(x_a, \mu_F) f_{b/h_2}(x_b, \mu_F)\, \mathrm{d}\hat{\sigma}_{ab\to n}(\mu_F, \mu_R)$$

$f_a(x)$ = probability of finding parton a in the particle h with longitudinal momentum fraction x

Leptons are "cleaner" than hadrons because $f(x) \sim$ □$(x-1)$*

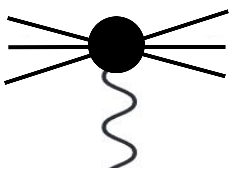
Useful Application: **Weizsäcker-Williams****

Process with a t-channel photon



$\underset{t\to 0}{=}$

On-shell photon amplitude



× Propagator $1/t$ ×

Photon PDF / "Flux Factor"

*But not exactly, which leads to lots of fun with gauge bosons and jets!
**Sometimes called the "Effective Photon Approximation" or "Effective Vector Approximation"

Not included: Heavy ion experiments, neutrino experiments, *ep* experiments, astronomical or cosmological observations…

Why Muons?

"This is our Muon Shot"

1. Achieve *much* **higher energies** than e^+e^-
2. **Cleaner*** than *pp* collisions
3. "**Electroweak** Boson Collider"
4. Direct probe of **2nd gen physics**
5. "It's just [redacted]**ing cool**" – Nima Arkani-Hamed, APS 2023

Road to the Future

Lots of R&D needed! A huge undertaking …

This Talk: R&D is worth it, because **muon test beams** already have the potential for discovering **new physics**! Interesting results for muon beams as low as **10 GeV**!